## THE SHAPES OF GRAPHS AND ABSOLUTE EXTREMES

1. Sketch the graph of a function y = f(x) such that all of the following are true:

a) f'(-2) = 0 and f''(-2) > 0b) f(0) = 1, f'(0) = 0, and f''(0) < 0c) f'(3) > 0 and f''(3) < 0d)  $\lim_{x\to\infty} f(x) = 0$ 

**2.** Why does  $f(x) = x - \frac{1}{x}$  not have an absolute minimum on the interval (0, 2]? Does it have an absolute maximum?

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**3.** Find the absolute minimum and maximum of  $f(x) = x - 3x^{2/3}$  over the interval [-1, 10]. It may help to know that  $f(10) \approx -3.9248$ .