## THE SHAPES OF GRAPHS AND ABSOLUTE EXTREMES

1. Sketch the graph of a function $y=f(x)$ such that all of the following are true:
a) $f^{\prime}(-2)=0$ and $f^{\prime \prime}(-2)>0$
b) $f(0)=1, f^{\prime}(0)=0$, and $f^{\prime \prime}(0)<0$
c) $f^{\prime}(3)>0$ and $f^{\prime \prime}(3)<0$
d) $\lim _{x \rightarrow \infty} f(x)=0$

2. Why does $f(x)=x-\frac{1}{x}$ not have an absolute minimum on the interval ( 0,2$]$ ? Does it have an absolute maximum?
3. Find the absolute minimum and maximum of $f(x)=x-3 x^{2 / 3}$ over the interval $[-1,10]$. It may help to know that $f(10) \approx-3.9248$.
