

To sketch $y = f(x)$:

1. **Domain.** Where is the function defined?

2. **Intercepts.** y -intercept at $f(0)$. x -intercept(s) by solving $f(x) = 0$ for x .

3. **Symmetry.**

Even if $f(-x) = f(x)$ for all x in the domain. y -axis symmetry.

Odd if $f(-x) = -f(x)$ for all x in the domain. Origin symmetry.

Periodic if it repeats (like $y = \sin x$ or graphs of other trig functions).

4. **Asymptotes.**

Horizontal (if any) at $\lim_{x \rightarrow \infty} f(x)$ and $\lim_{x \rightarrow -\infty} f(x)$.

Vertical (if any) at places where $\lim_{x \rightarrow a^+} f(x) = \pm\infty$ or $\lim_{x \rightarrow a^-} f(x) = \pm\infty$ (watch for division by 0). Determine how the function approaches any asymptotes.

5. **Increasing/Decreasing.** Use the first derivative.

6. **Local Extremes.** Use the information from the previous step.

7. **Concavity and Inflection Points.** Use the second derivative.

8. **Draw it.**

Examples:

1. $y = (x^2 - 1)^3$

2. $y = \frac{x}{x^3 - 1}$

3. $y = x^{\frac{2}{3}}(6 - x)^{\frac{1}{3}}$