1. Find the absolute maximum and minimum values of  $f(x) = x^3 - 6x^2 + 9x + 2$  over the interval [0, 2].

- 2. Find the absolute maximum and absolute minimum values of  $f(x) = \frac{x^3-2}{x^3+2}$  over the interval [-1,3]
- **3.** Sketch the graph of  $f(x) = \frac{x}{1+x^2}$ . Clearly indicate the location of all axis intercepts, asymptotes, and local extrema.
- 4. The graph of the derivative of a function (y = f'(x)) is shown.



- a) At what value(s) of x does the function f have a local maximum?
- d) On what interval(s) is the graph of the function y = f(x) concave downward?
- 5. Find the interval(s) on which the function  $f(x) = 2 + 3x^2 x^3$  is concave upward.

6. Let  $g(x) = \sqrt{1 - x^2}$ . Use the Mean Value Theorem to show that g'(c) = 1 for some c in the interval [-1, 0] or explain why the Mean Value Theorem does not apply.

7. Use Newton's method with initial approximation  $x_1 = -1$  to find the second approximation,  $x_2$ , of a solution to the equation  $x^5 + 2 = 0$ .

8. Explain why  $x_1 = 1$  is a poor starting guess when Newton's method is used to find the root of the function whose graph is shown.



9. Find the most general form of an antiderivative of  $f(x) = \sqrt{x} - \frac{2}{x^2}$ 

10. A particle in a magnetic field has velocity  $v(t) = \sin t \, \text{m/s}$  and at time 0 its position is 0. Find a function giving the position of the particle at time t.

11. Find the dimensions of a rectangle with perimeter 80m whose area is as large as possible. Verify that your answer is a maximum.

12. A box with square base and an open top is to have a volume of  $10m^3$ . Material for the base costs \$10 per square meter and material for the sides costs \$8 per square meter. Determine the dimensions of the cheapest such container. Verify that your answer is a minimum.