1. Find the absolute maximum and minimum values of the function over the interval:

a) 
$$f(x) = (x^2 - 1)^3$$
,  $[-2, 1]$ 

b) 
$$f(x) = x^3 - 6x^2 + 9x + 2$$
,  $[-2, 3]$ 

c) 
$$f(x) = x + \cos x$$
,  $[0, 2\pi]$ 

d) 
$$f(x) = |\sin x|, [-\frac{\pi}{2}, \pi]$$

**2.** Prove that  $f(x) = x^3 + x^2 + x + 1$  has no local extremes.

3. Prove that  $f(x) = x^{101} + x^{51} + x + 1$  has no local extremes.