

1. Find the volume of the solid that lies under the hyperbolic paraboloid $z = 3y^2 - x^2 + 2$ and above the rectangle $R = [-1, 1] \times [1, 2]$.
2. Find the volume of the solid enclosed by the surface $z = 1 + e^x \sin y$ and the planes $x = \pm 1$, $y = 0$, $y = \pi$, and $z = 0$.
3. Find the volume of the solid under the surface $z = 1 + x^2y^2$ and above the region enclosed by $x = y^2$ and $x = 4$.
4. Find the volume of the solid bounded by the cylinder $y^2 + z^2 = 4$ and the planes $x = 2y$, $x = 0$, $z = 0$ in the first octant.
5. Reverse the order of integration for the integral $\int_0^2 \int_{x^2}^4 f(x, y) dy dx$.
6. Evaluate the integral by reversing the order of integration $\int_0^{\sqrt{\pi}} \int_y^{\sqrt{\pi}} \cos(x^2) dx dy$.
7. Find the area of the polar region $R = \{(r, \theta) \mid 0 \leq r \leq 2 \sin \theta, \frac{\pi}{2} \leq \theta \leq \pi\}$.
8. Evaluate the integral $\iint_A \sin(x^2 + y^2) dA$ where A is the region enclosed by the circle $x^2 + y^2 = 4$ and the lines $x = 0$ and $y = x$.
9. Determine the volume of the solid below the paraboloid $z = 18 - 2x^2 - 2y^2$ and above the xy -plane.
10. Find the center of mass of the lamina that occupies the region enclosed by the lines $x = 0$, $y = x$, and $2x + y = 6$ and has density function $\rho(x, y) = x^2$.
11. A lamina occupies the region inside the circle $x^2 + y^2 = 2y$ but outside the circle $x^2 + y^2 = 1$ and has density $\rho(x, y) = \frac{1}{\sqrt{x^2 + y^2}}$. Find the center of mass of the lamina.
12. Evaluate the integral $\iiint_E \sin y dV$ where E is the region below the plane $z = x$ and above the triangular region with vertices $(0, 0, 0)$, $(\pi, 0, 0)$, and $(0, \pi, 0)$.
13. Find the center of mass of the solid bounded by the parabolic cylinder $z = 1 - y^2$ and the planes $x + z = 1$, $x = 0$, and $z = 0$ and with density function $\rho(x, y, z) = 4$.
14. Find the moments of inertia of a rectangular brick with dimensions a , b , and c , mass M , and constant density if the center of the brick is at the origin and the edges are parallel to the coordinate axes.
15. Evaluate $\iiint_E x dV$ where E is the solid enclosed by the planes $z = 0$ and $z = x + y + 5$ and by the cylinders $x^2 + y^2 = 4$ and $x^2 + y^2 = 9$.
16. Evaluate $\iiint_H 9 - x^2 - y^2 dV$ where H is the solid hemisphere $x^2 + y^2 + z^2 \leq 9$, $z \geq 0$.
17. Find the centroid of the solid (with uniform density 1) inside $x^2 + y^2 + z^2 = 4$, outside $x^2 + y^2 + z^2 = 1$ and above $z = 0$.
18. Find the Jacobian of the transformation $x = v$, $y = u(1 + v^2)$.
19. Use the transformation $x = \frac{1}{4}(u + v)$, $y = \frac{1}{4}(v - 3u)$ to evaluate the integral $\iint_R 4x + 8y dA$ where R is the parallelogram with vertices $(-1, 3)$, $(1, -3)$, $(3, -1)$, and $(1, 5)$.