

INSTRUCTIONS: Solve 6 of the 7 problems; choose one problem to skip and put a big **X** in the corresponding box below. If you do not indicate which problem you are choosing to skip, I will assume that I should skip problem 7, which may hurt your grade. Show your work: even correct answers may receive little or no credit if a method of solution is not shown. You do not need to simplify your solutions. Graphing calculators, notes, cell phones, and other materials are not permitted.

Name:							
1	2	3	4	5	6	7	Total

Theorems

$$\text{Green's (general): } \oint_C Pdx + Qdy = \iint_R \frac{\partial Q}{\partial x} - \frac{\partial P}{\partial y} dA$$

$$\text{Green's (circulation): } \oint_C \mathbf{F} \cdot d\mathbf{r} = \iint_R \frac{\partial g}{\partial x} - \frac{\partial f}{\partial y} dA$$

$$\text{Green's (flux): } \oint_C \mathbf{F} \cdot \mathbf{n} ds = \iint_R \frac{\partial f}{\partial x} + \frac{\partial g}{\partial y} dA$$

$$\text{Stokes': } \oint \mathbf{F} \cdot d\mathbf{r} = \iint_S (\nabla \times \mathbf{F}) \cdot \mathbf{n} dS$$

$$\text{Divergence: } \iint_S \mathbf{F} \cdot \mathbf{n} dS = \iiint_D \nabla \cdot \mathbf{F} dV$$

Test for conservative v.f.: \mathbf{F} is conservative if and only if $\text{curl}\mathbf{F} = 0$

Fundamental theorem of line integrals: if \mathbf{F} is conservative, then $\int_C \mathbf{F} \cdot d\mathbf{r} = \varphi(B) - \varphi(A)$

Definitions

$$\text{Curl (3-d): } \text{curl}\mathbf{F} = \nabla \times \mathbf{F} = \left\langle \frac{\partial h}{\partial y} - \frac{\partial g}{\partial z}, \frac{\partial f}{\partial z} - \frac{\partial h}{\partial x}, \frac{\partial g}{\partial x} - \frac{\partial f}{\partial y} \right\rangle$$

$$\text{Curl (2-d): } \text{curl}\mathbf{F} = \frac{\partial g}{\partial x} - \frac{\partial f}{\partial y}$$

$$\text{Divergence (3-d): } \text{div}\mathbf{F} = \nabla \cdot \mathbf{F} = \frac{\partial f}{\partial x} + \frac{\partial g}{\partial y} + \frac{\partial h}{\partial z}$$

$$\text{Divergence (2-d): } \text{div}\mathbf{F} = \nabla \cdot \mathbf{F} = \frac{\partial f}{\partial x} + \frac{\partial g}{\partial y}$$

Line integrals

Scalar: $\int_C f \, ds = \int_a^b f(\mathbf{r}(t)) |\mathbf{r}'(t)| \, dt$

Circulation/work: $\int_C \mathbf{F} \cdot d\mathbf{r} = \int_C f \, dx + g \, dy = \int_a^b \mathbf{F}(\mathbf{r}(t)) \cdot \mathbf{r}'(t) \, dt$

Flux: $\int_C \mathbf{F} \cdot \mathbf{n} \, ds = \int_C f \, dy - g \, dx = \int_a^b [f(\mathbf{r}(t))y'(t) - g(\mathbf{r}(t))x'(t)] \, dt$

Surface integrals

Scalar: $\iint_S f \, dS = \iint_R f(\mathbf{r}(u, v)) |\mathbf{t}_u \times \mathbf{t}_v| \, dA$

Scalar for $z = z(x, y)$: $\iint_S f \, dS = \iint_R f(x, y, z(x, y)) \sqrt{z_x^2 + z_y^2 + 1} \, dA$

Flux: $\iint_S \mathbf{F} \cdot \mathbf{n} \, dS = \iint_R \mathbf{F} \cdot (\mathbf{t}_u \times \mathbf{t}_v) \, dA$

Flux for $z = z(x, y)$: $\iint_S \mathbf{F} \cdot \mathbf{n} \, dS = \iint_R \mathbf{F} \cdot \langle -z_x, -z_y, 1 \rangle \, dA = \iint_R (-f z_x - g z_y + h) \, dA$

Integration formulas from Ch. 13

Applications	Translations		Differentials
$A = \iint_R dA$	Rectangular \rightarrow Cylindrical	Rectangular \rightarrow Spherical	$dV = \dots$
$V = \iint_R f(x, y) \, dA$	$x = r \cos \theta$	$x = \rho \sin \varphi \cos \theta$	$dx \, dy \, dz$
$m = \iint_R f(x, y) \, dA$	$y = r \sin \theta$	$y = \rho \sin \varphi \sin \theta$	$r \, dz \, dr \, d\theta$
$V = \iiint_S dV$	$z = z$	$z = \rho \cos \varphi$	$\rho^2 \sin \varphi \, d\rho \, d\varphi \, d\theta$
$m = \iiint_S f(x, y, z) \, dV$	$x^2 + y^2 = r^2$	$x^2 + y^2 + z^2 = \rho^2$	