**Theorem.** If  $y_p$  is any solution to the differential equation

$$y'' + p(x)y' + q(x)y = f(x)$$
(1)

and  $\{y_1,y_2\}$  is a fundamental set of solutions to the complementary equation y''+p(x)y'+q(x)y=0, then a general solution for differential equation 1 is

$$y = y_p + c_1 y_1 + c_2 y_2$$

- 1. Consider the differential equation  $y'' 7y' + 12y = 4e^{2x}$ .
- a) Find a constant A such that  $y_p = Ae^{2x}$  is a solution of the differential equation.

b) Find a general solution for the differential equation.

- **2.** Consider the differential equation  $y'' 7y' + 12y = 5e^{4x}$ .
- a) Why can't you find a constant A such that  $y_p=Ae^{4x}$  is a solution for the differential equation?

b) Find a constant $B$ such that $Bxe^{4x}$ is a solution for the differential equation.
c) Find a general solution for the differential equation.
<b>Theorem</b> (Superposition). If $y_{p_1}$ is a particular solution of $y'' + p(x)y' + q(x)y = f_1(x)$ and $y_{p_2}$ is a particular solution of $y'' + p(x)y' + q(x)y = f_2(x)$ , then a particular solution of
$y'' + p(x)y' + q(x)y = f_1(x) + f_2(x)$
is $y_p=y_{p_1}+y_{p_2}$
<b>3.</b> Use the principle of superposition to find a general solution to the differential equation $y''-7y'+12y=5e^{4x}+4e^{2x}$ .
<b>4.</b> Consider the differential equation $y'' - 8y' + 16y = 2e^{4x}$ .
a) Why can't you find a constant $A$ such that $y_p = Ae^{4x}$ is a solution of the differential equation?
b) Why can't you find a constant $B$ such that $Bxe^{4x}$ is a solution of the differential equation?
c) Find a constant $C$ such that $Cx^2e^{4x}$ is a solution of the differential equation.
d) Find a general solution for the differential equation.