

**Method** (Power series solutions for  $P_0(x)y'' + P_1(x)y' + P_2(x)y = 0$ ). If  $P_0(x_0) \neq 0$ , then we'll say that  $x_0$  is an **ordinary point** of the differential equation. We seek a power series solution centered at  $x_0$ :

$$y = \sum_{n=0}^{\infty} a_n(x - x_0)^n = a_0 + a_1(x - x_0) + a_2(x - x_0)^2 + a_3(x - x_0)^3 + \dots$$

Using these in our differential equation gives recursive formulas for the coefficients. Note that  $y(x_0) = a_0$  and  $y'(x_0) = a_1$ . Thus, initial values for  $y(x_0)$  and  $y'(x_0)$  allow us to find values for all the coefficients.

**Comment.** The method works at any ordinary point, but we'll usually work with  $x_0 = 0$ .

**1.** Using  $x_0 = 0$ , write out power series for  $y$ ,  $y'$ , and  $y''$ . Either use sigma notation or expand each series to the  $x^3$  term.

When you're finished with (or stuck on) problem 1, watch the video example.

**2.** Find the first 4 coefficients of a series solution to the IVP  $(1 + x^2)y'' + 6xy' + 6y = 0$ ,  $y(0) = -1$  and  $y'(0) = 1$ .

**3.** Find the first 4 coefficients of a series solution to the IVP  $(1 + 8x^2)y'' + 2y' = 0$ ,  $y(0) = 2$  and  $y'(0) = -1$ .