

SOLVING IVPs USING LAPLACE TRANSFORMS

Theorem. Suppose f and f' are continuous on $[0, \infty)$ and of exponential order s_0 , and that f'' is piecewise continuous on $[0, \infty)$. Then f , f' , and f'' have Laplace transforms for $s > s_0$:

$$\boxed{L(f') = sL(f) - f(0)} \text{ and } \boxed{L(f'') = s^2L(f) - sf(0) - f'(0)}$$

Method. How to use Laplace transforms to solve an IVP:

- 1) Take the Laplace transform of the differential equation
- 2) Use the initial conditions
- 3) Solve for $Y = L(y)$ (do as little algebra as possible)
- 4) Take the inverse Laplace transform to find y

1 (Completion). Use Laplace transforms to solve the following IVPs:

- a) $y'' + y' - 2y = 2e^{3t}$, $y(0) = -1$, $y'(0) = 4$
- b) $y'' - 4y' + 4y = 1$, $y(0) = 0$, $y'(0) = 1$ (be careful with the partial fractions decomposition in this one)