

1. Make a truth table for the expression $P \implies (P \vee Q)$.
2. Write the following expression (Bertrand's postulate) in English:

$$(\forall n \in \mathbb{N})(\exists p \in \mathbb{N}) [(p \text{ is prime}) \wedge (n < p < 2n)].$$

3. Is it true that $\{x \in \mathbb{R} : x^2 \leq 1\} \subseteq \{x^2 : x \in \mathbb{R}\}$?
4. Find all integer solutions to the equation $x^2 \equiv 1 \pmod{3}$.
5. Prove that if 1 is even, then 0.5 is an integer.
6. Let $a, b \in \mathbb{Z}$. Prove that if ab is even, then either a or b is even.
7. Let $a \in \mathbb{N}$. Prove that if $2^a - 1$ is prime, then a is odd or $a = 2$.
8. Is the converse of the statement in problem 7 true?
9. Determine if the following statement is true or false:

$$(\forall a, b \in \mathbb{N})(\exists d \in \mathbb{N}) [(d|a \wedge d|b) \wedge ((\forall x \in \mathbb{N})(x|a \wedge x|b) \implies x \leq d)].$$