

$$1. a) E(\bar{X} - \bar{Y}) = \mu_1 - \mu_2 \quad \text{Var}(\bar{X} - \bar{Y}) = \frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}$$

$$b) \bar{X} - \bar{Y} \pm Z_{\alpha/2} \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}$$

$$c) 2258 - 2637 - 2.326348 \sqrt{\frac{(1519)^2}{663} + \frac{(1138)^2}{413}} \approx -568.22$$

We are 99% confident that eating fast food regularly adds no more than 568.22 calories on average.

Note:  $2637 - 2258 - 2.326348 \sqrt{\frac{(1138)^2}{413} + \frac{(1519)^2}{663}}$  is also a reasonable answer.

$$2. s_p^2 = \frac{23(.13)^2(24) + 29(.12)^2(30)}{52} \approx .4203$$

$$95\% \text{ CI: } .10 - (-.96) \pm 2.006647 (.6483) \sqrt{\frac{1}{24} + \frac{1}{30}}$$

$$(.7037, 1.4163)$$

3. Test abdominal fat for Resistance Exercise vs. Aerobic Exercise

$$s_p^2 = \frac{29(.11)^2(30) + 29(.13)^2(30)}{58} = .435$$

$$t = \frac{-.42 - (-.84)}{\sqrt{.435(\frac{1}{30} + \frac{1}{30})}} \approx 2.4663$$

$$P\text{-value: } 2P(T \geq 2.4663) = .0166$$

Reject  $H_0: \mu_1 - \mu_2 = 0$  in favor of  $H_1: \mu_1 - \mu_2 \neq 0$  at sig level 0.05.  
Aerobic exercise is better at getting rid of fat.